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First principles of Ca²⁺-signal decoding

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Abstract

Calcium (Ca²⁺) is an important signaling molecule in cellular processes. In resting conditions, Ca²⁺ is actively exported from the cell resulting in very low cellular Ca²⁺ concentrations. External stimuli (as touch, damage, temperature change, ?) induce oscillations in cellular Ca²⁺. These Ca²⁺-oscillations activate or deactivate proteins, which in turn modifies diverse cellular processes.

Coding and decoding of Ca²⁺-signals is poorly understood. I approached this topic by describing the physico-chemical principles of the interaction of Ca²⁺ and proteins in mathematical terms. A characteristic differential equation type $\left[\frac{df}{dt} = A - B * f\right]$ plays a dominant role in the decoding process [A and B depend on the Ca²⁺-concentration in a non-linear manner]. Cellular modules that follow this equation type allow the readout of frequency and amplitude information from the Ca²⁺-signal.

The problem that I would like to discuss with mathematicians is: In biology oscillations are exclusively approached with Fourier-analysis, which is based on periodic trigonometric functions. I do not find that this is an appropriate approach. The representation of the Ca²⁺-signal as a sum of rectangular functions would be more appropriate. In this case A and B are constant (even though for short time intervals) and the equation $\frac{df}{dt} = A - B * f$? can be solved.

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